

324553(24)

B. E. (Fifth Semester) Examination,
April-May 2016

(New Scheme)

(Elect. Engg. Branch)

APPLIED NUMERICAL ANALYSIS*Time Allowed : Three hours**Maximum Marks : 80**Minimum Pass Marks : 28*

Note : Attempt all questions. Part (a) is compulsory of 2 marks. Attempt any two parts from (b), (c) and (d) is of 7 marks.

Unit-I

- (a) What is approximate numbers? 2
- (b) Prove the following useful results from the Newton's iteration formula : 7

324553(24)

PTO

- (i) Iterative formula to find $\frac{1}{N}$ is

$$x_{n+1} = x_n(2 - Nx_n)$$

- (ii) Iterative formula to find $\sqrt[k]{N}$ is

$$x_{n+1} = \frac{1}{K} \left[(K-1)x_n + N/x_n^{k-1} \right]$$

- (c) Using Newton's iterative method, find the real root of $x \log_{10} x = 1.2$ correct to five decimal places. 7
- (d) Find a not of the equation $x - e^x = 0$ correct to three decimal places by the secant method. 7

Unit-II

2. (a) What is eigen values and eigen vector? 2
- (b) Solve : 7

$$10x - 7y + 3z + 5u = 6$$

$$-6x + 8y - z - 4u = 5$$

$$3x + y + 4z + 11u = 2$$

$$5x - 9y - 2z + 4u = 7$$

by Gauss elimination method.

324553(24)

[3]

- (c) Apply Gauss Jordan method to solve the equations : 7

$$x + y + z = 9$$

$$2x - 3y + 4z = 13$$

$$3x + 4y + 5z = 40$$

- (d) Explain Jacobi iteration and Gauss seidal-iteration method. 7

Unit-III

3. (a) Define interpolation. 2
 (b) Explain weierstrass approximation theorem. 7
 (c) Derive Newton's forward interpolation formula. 7
 (d) A curve passes through the points (0, 18), (1, 10), (3, -18) and (6, 90) find the slope of the curve at $x = 2$ by using Langrange's formula. 7

Unit-IV

4. (a) Define numerical integration. 2
 (b) Calculate the first and second derivatives of the functions tabulated below at the point $x = 1.1$: 7
- | | | | | | | |
|------------|-------|-------|-------|-------|-------|------|
| x | : 1.0 | 1.2 | 1.4 | 1.6 | 1.8 | 2.0 |
| $y = f(x)$ | : 0 | 0.128 | 0.544 | 1.296 | 2.432 | 4.00 |

324553(24)

PTO

[4]

- (c) Determine derivatives using backward difference formula. 7
 (d) Derive Newton cotes quadrature formula. 7

Unit-V

5. (a) What is ordinary differential equation? 2
 (b) Explain modified Euler's method. 7
 (c) Apply Runge Kutta method to find approximate value of y for $x = 0.2$, in steps of 0.1 if $\frac{dy}{dx} = x + y^2$ given that $y = 1$ where $x = 0$. 7
 (d) Solve by Taylor series method of third order the equation

$$\frac{dy}{dx} = \frac{x^3 + xy^2}{e^x}, y(0) = 1$$

for y at $x = 0.1, x = 0.2$ and $x = 0.3$. 7

350]

324553(24)